

# **Task Group**

## **for the Development of IAPWS–IF97 Backward Equations in Region 3**

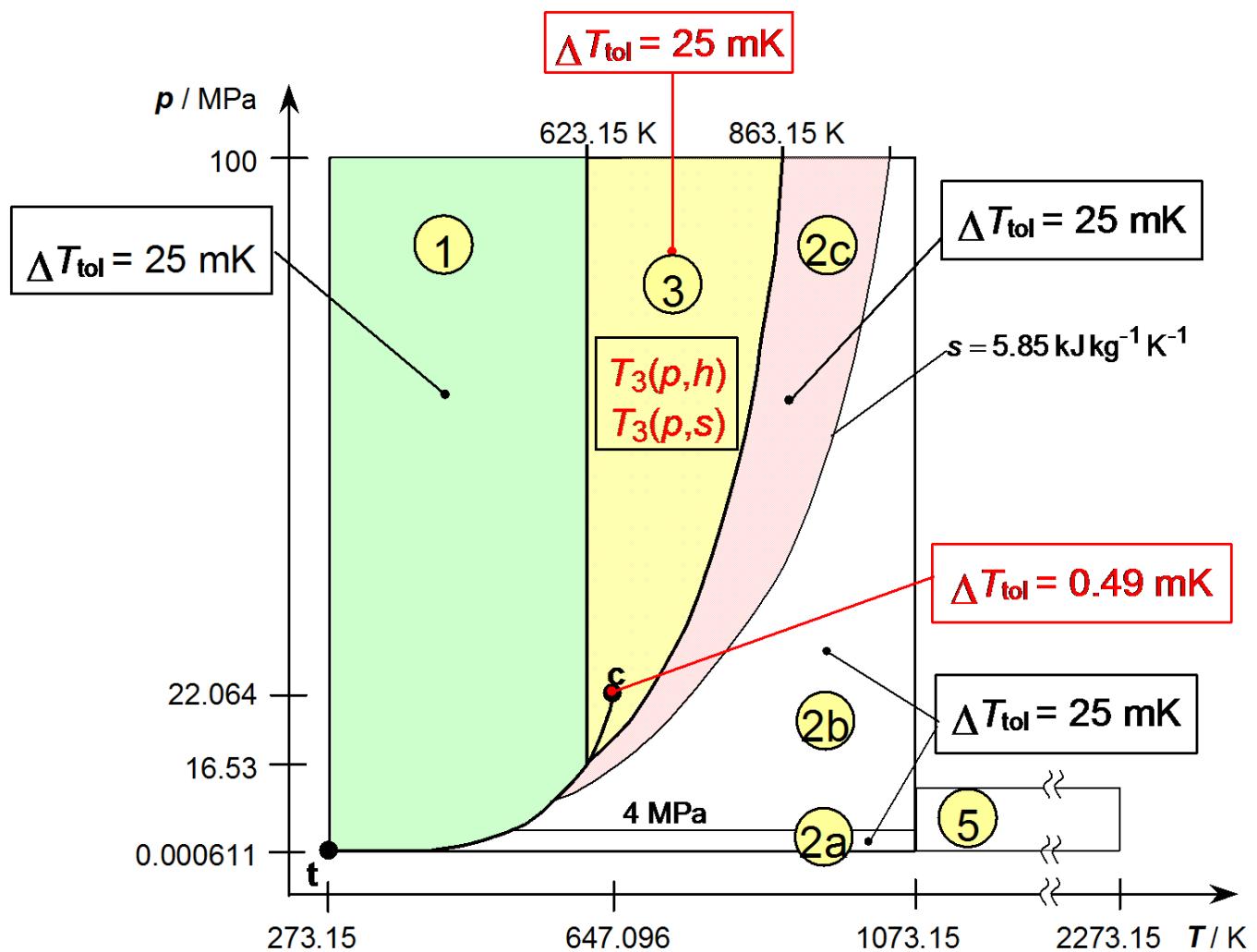
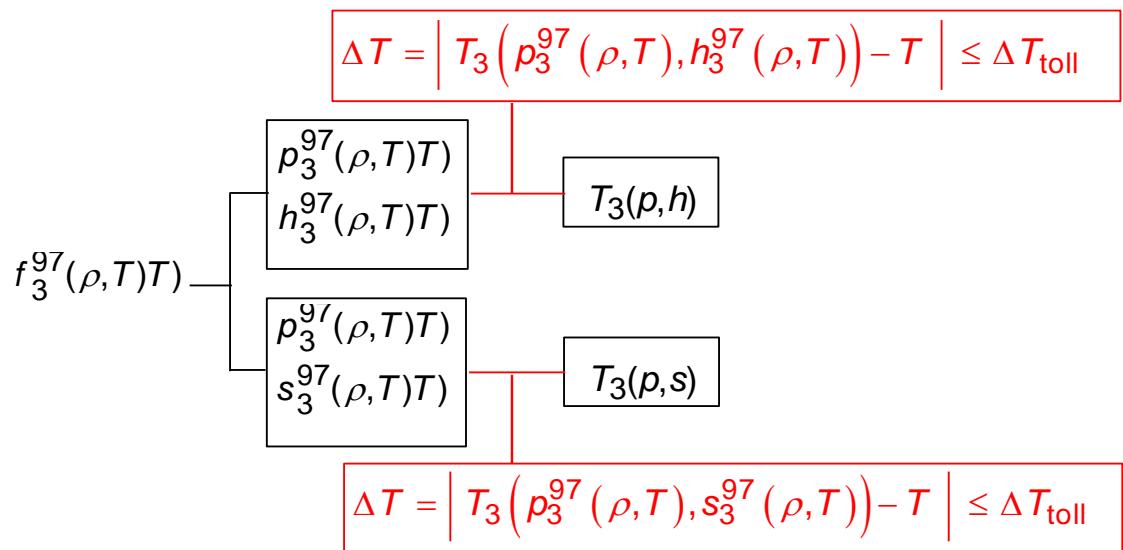
- Current Members: Hans-Joachim Kretzschmar (Chair)  
Radim Mareš  
Wolfgang Wagner
- Progress Report:  
K. Knobloch, I. Stöcker, H.-J. Kretzschmar, A. Dittmann:  
Development of Supplementary Backward Equations  $T(p,h)$  and  
 $T(p,s)$  for the Critical and Supercritical Regions of Water and Steam.
- Specifications for the Equations  $T(p,h)$  and  $T(p,s)$
- Name of the Task Group
- Membership
- Time Schedule

# **Proposal**

## **Specifications for the Supplementary Backward Equations $T(p,h)$ and $T(p,s)$ in Region 3 of IAPWS-IF97**

1. Numerical Consistency with IAPWS-IF97
2. Numerical Consistency at Boundaries Between Subregions
3. Computing Time in Relation to IAPWS-IF97

## 1. Numerical Consistency with IAPWS-IF97



## Numerical Consistency with IAPWS-IF97

Equations  $T_3(p,h)$ :

$$\Delta T = \left| T_3(p_3^{97}(\rho, T), h_3^{97}(\rho, T)) - T \right| \leq 25 \text{ mK}$$

Equations  $T_3(p,s)$ :

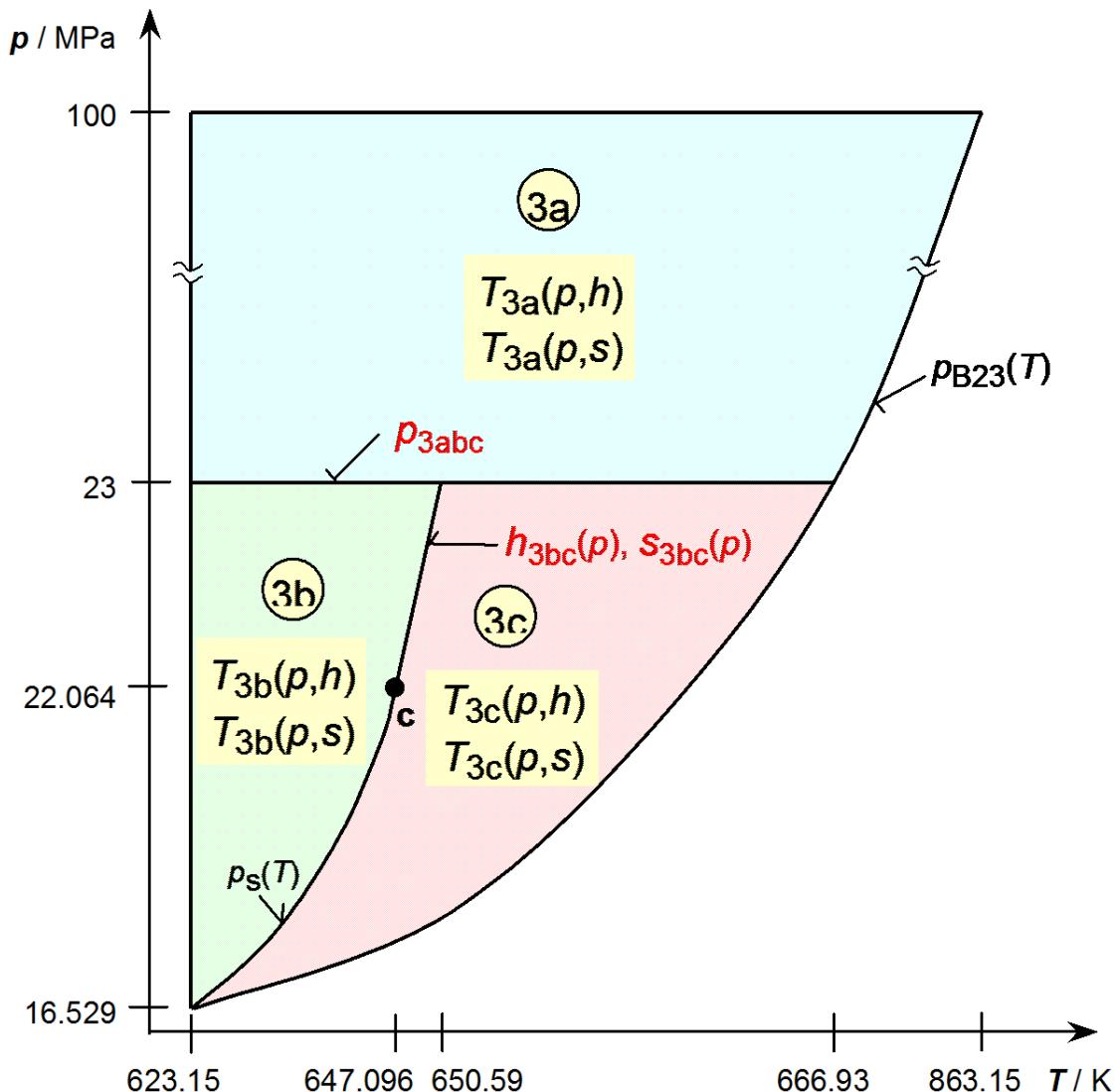
$$\Delta T = \left| T_3(p_3^{97}(\rho, T), s_3^{97}(\rho, T)) - T \right| \leq 25 \text{ mK}$$

Exception

At critical point the value 647.096 K should be calculated.

$$\Delta T \leq 0,49 \text{ mK}$$

## 2. Numerical Consistency at Boundaries Between Subregions



Subregion boundary:

$$\left. \begin{array}{l} p_{3abc} \\ h_{3bc}(p) \\ s_{3bc}(p) \end{array} \right\} \quad \begin{array}{l} \text{Numerical Differences between} \\ \text{adjacent backward equations:} \\ \boxed{\Delta T \leq 25 \text{ mK}} \end{array}$$

### 3. Computing Time in Relation to IAPWS-IF97

#### Computing Time Ratio - *CTR* Value

$$CTR = \frac{\text{Computing time of IAPWS-IF977}}{\text{Computing time of new equations}}$$

Calculation of  $T_3(p,h)$ :  $CTR > 10$

Calculation of  $T_3(p,s)$ :  $CTR > 10$

## **Proposal for the name of the Task Group**

Task Group on Supplementary Backward Equations for  
Region 3 of IAPWS-IF97

## **Time Schedule for the Development of the Equations $T(p,h)$ and $T(p,s)$ in Region 3**

### **IAPWS Annual Meeting 2001**

- Discussion of the specifications
- Presentation of first results

### **IAPWS Annual Meeting 2002**

- Presentation of the final set of equations
- Evaluation Task Group can begin to work

### **IAPWS Annual Meeting 2003**

- Adoption of the equation set

## Computing Time Investigations

### Iterative Calculation of $p$ & $T(h,s)$ Using IF97 Equations Only

Two-dimensional  
Iteration of  $p$  and  $T$   
from:  $s = s^{97}(p, T)$   
 $h = h^{97}(p, T)$

### Calculation of $p, T(h,s)$ Using the New $p(h,s)$ Equations

$$\begin{array}{c} p = p(h,s) \\ \downarrow \\ T = T^{97}(p,h) \end{array}$$

### Result

The calculation speed is between 10 and 30 times faster than that of the 2-dimensional Newton method, depending on iteration starting values and iteration algorithm.

## Summary

Supplementary Release on  $p(h,s)$  equations is ready  
for adoption by IAPWS